

# **Algorithmic Sustainable Design: The Future of Architectural Theory.**

Nikos A. Salingaros  
University of Texas at San Antonio

*Notes from a series of 12 lectures applying cutting-edge mathematical techniques to architectural and urban design.*

© 2008, 2009, Nikos A. Salingaros & Umbau-Verlag, Solingen, Germany.

## **Contents**

1. Recursion and the Fibonacci sequence. Universal scaling. Biophilia.
2. Geometric Recursion and Fractals: the Sierpinski gasket. Perforation, bending, and folding. Anti-gravity anxiety. Architecture of the horizontal.
3. Universal distribution of sizes. Fractal design, ornament, and biophilia. Sustainable systems.
4. Cellular automata. Sierpinski carpets and sea-shells. Design in hyperspace and connection to the sacred.
5. Architectural harmony. Christopher Alexander's theory of centers. Design as computation. Computational reducibility.
6. Alexander's 15 Fundamental Properties. Three laws of architecture.
7. Biologically-inspired computation. Genetic algorithms. Computation versus memory retrieval. Evolutionary regression.
8. Emergent systems. Examples from Artificial Life. Inhuman experiments. Architectural education.
9. Symmetry production. Symmetry breaking. Classical moldings. Elementary particle symmetries. Binding energy.
10. Generative codes and their application to building and urban morphology. Secularization destroys public space. Spiritual architects. Legalizing codes.
11. Duany-Plater-Zyberk (DPZ) codes. The New Urbanism. Stephen Mouzon's project. Tall buildings.
12. Implementation of generative codes in design. Urban plazas. Designing for children. Favelas and social housing.

## **Texts**

I refer to the monograph “Harmony-seeking computations” by Christopher Alexander, to appear in the *International Journal of Unconventional Computation*, 2009, draft available from <[www.livingneighborhoods.org/library/harmony-seeking-computations.pdf](http://www.livingneighborhoods.org/library/harmony-seeking-computations.pdf)>. I also use Alexander’s “The Nature of Order”, Books 1, 2, 3, and 4, and Stephen Wolfram’s “A New Kind of Science”.

### **Lectures given over twelve weeks in the spring of 2008.**

Each one-hour lecture was repeated twice a week. The first time around, it was offered on Wednesdays at Michael G. Imber Architects, 111 W. El Prado St., San Antonio, Texas 78212. The lecture was repeated on Thursdays at The University of Texas at San Antonio, (1604 Campus), One UTSA Circle, San Antonio, Texas 78249. The Thursday lecture was transmitted via videoconference to participating institutions throughout the world.

## **Lecture 1**

### **1.1. Recursion and the Fibonacci sequence.**

### **1.2. Universal scaling.**

### **1.3. Biophilia.**

#### **1.1. Recursion and the Fibonacci sequence.**

##### Algorithmic design

- An algorithm is a set of instructions that can be followed to achieve a desired, but not always pre-determined end result
- Goes through successive states
- Breaks up the problem into smaller steps
- Sometimes uses recursive feedback
- Contrast with a conception of “all at once”

##### Design as computation

- We use algorithms to compute a result
- In the absence of an algorithm, we retrieve a result from memory — such computation is therefore based on what is stored in memory
- In architecture, memory of typology influences the results of new designs
- An algorithm makes us independent of memory, hence more creative

##### Sustainable design

- Use morphogenetic rules that nature follows
- Mimic but not copy physical, and especially biological structures

- The limitations of natural materials constrain built forms to certain geometries
- **Sticking on a solar panel does not connect to the intrinsic geometry of nature!**

#### Arithmetic Recursion

- A repeated operation with feedback
- Fibonacci sequence:
- Start with the number 1, then add 1
- Continue adding the previous two numbers to obtain the infinite sequence
- 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, ...

#### Universal Scaling Hierarchy

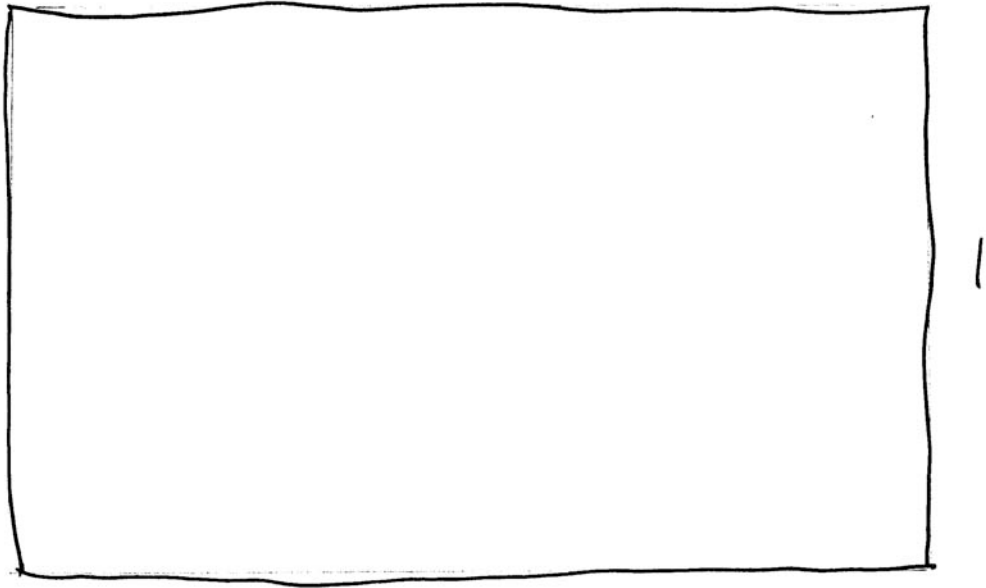
- We already have the mathematical tools for a fundamental result in architecture
- “The alternate terms of the Fibonacci sequence are a check for subdivisions in an adaptive design”
- {1, 3, 8, 21, 55, 144, 377, 987, 2584, ... }

#### Applications to design. (i) Going up in scale

- Take the smallest built scale, e.g. a step. Then, the next larger scale should be about 3 times that step, the next largest about 8 times the step, the next about 21 times the step, the next about 55 times, etc., going up to the size of the whole building
- The design should try to avoid significant scales in-between these approximate scales

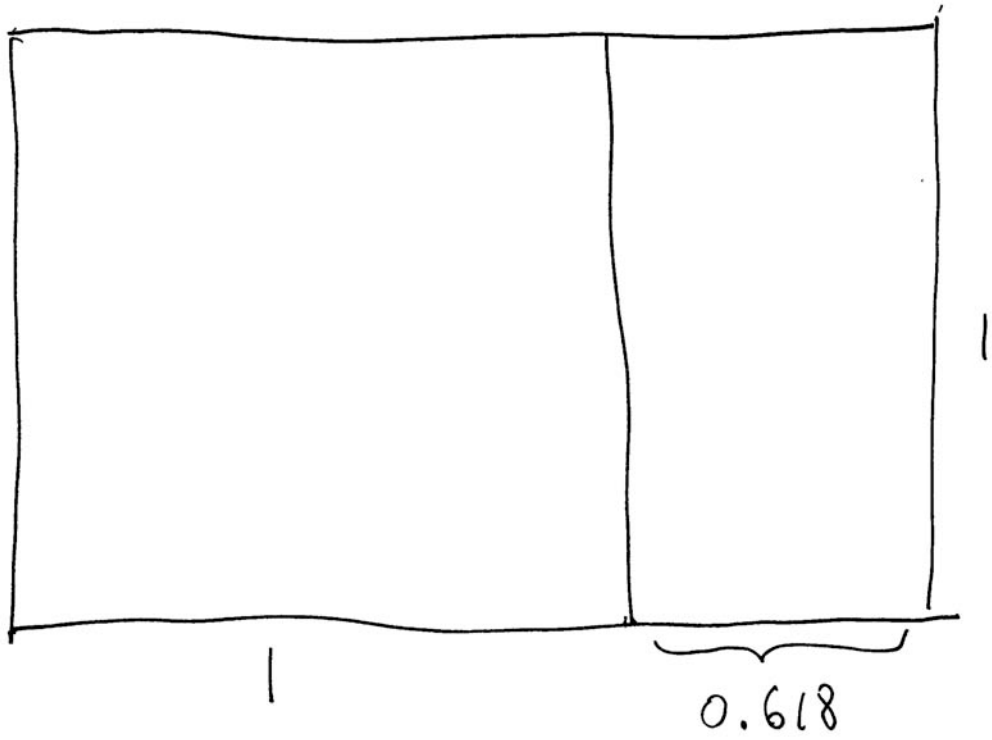
#### Applications to Design. (ii) Going down in scale

- Take the largest built scale, e.g. the building or its main feature. The next smaller scale should be about 1/3 of the largest dimension, the next smallest about 1/8 times the largest dimension, the next 1/21 of the largest dimension, etc., going right down to the size of small details
- There should be no significant scales in-between these scales

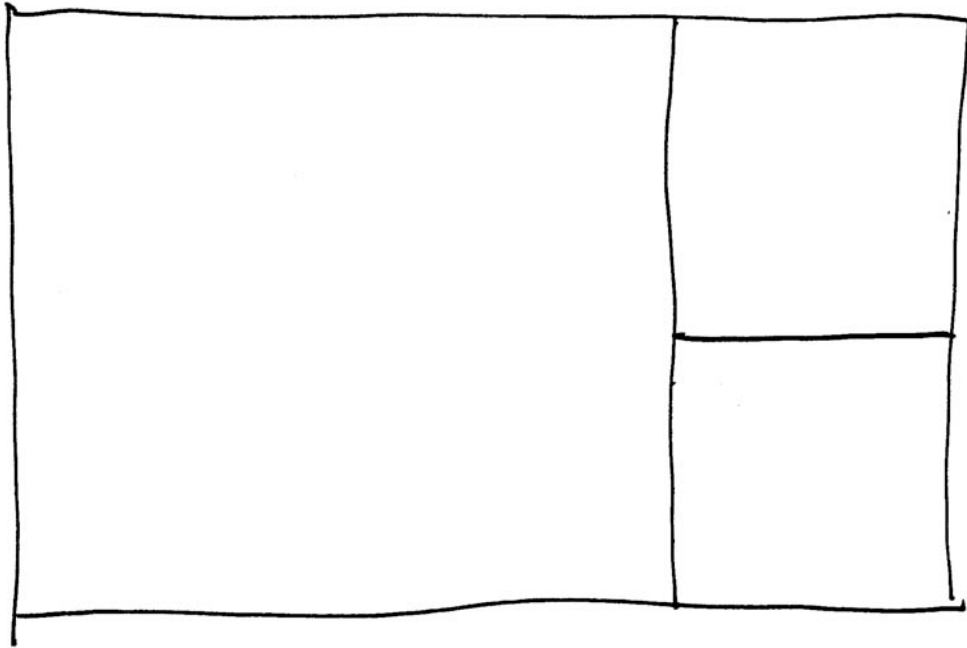


1.618

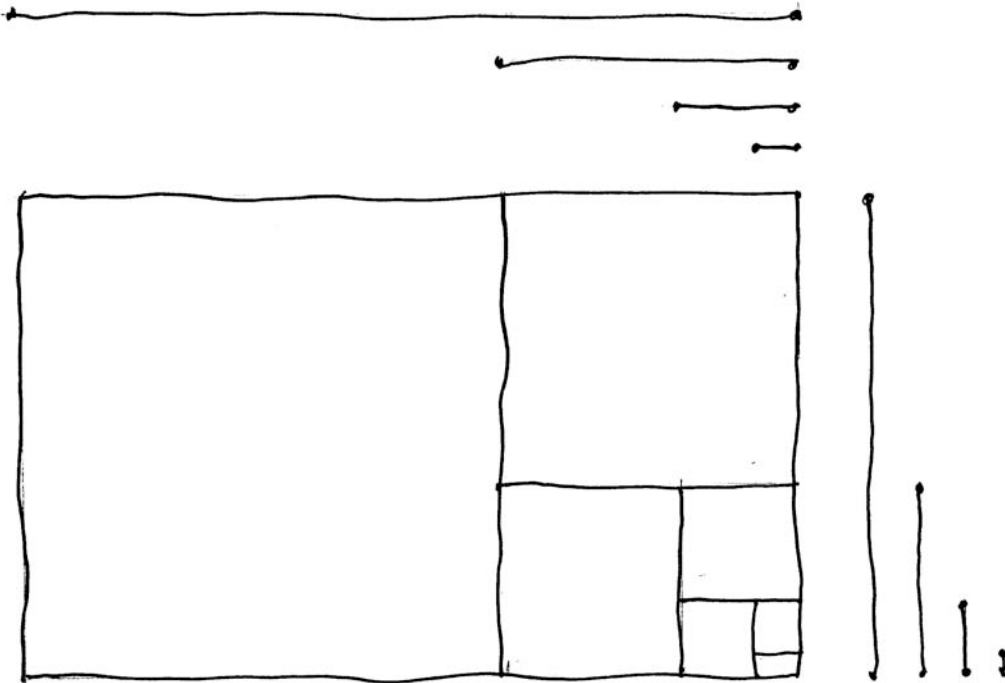
*The Golden Rectangle*



*Subdividing into a square plus a vertical golden rectangle*



*Two subdivisions generate a similar horizontal rectangle*



### *Universal scaling lengths*

#### Mathematical scaling ratio

- The limit of the ratio of alternate terms of the Fibonacci sequence as the terms get large is a fixed irrational number, 2.618
- Nevertheless, one cannot use powers of 2.618 instead of the integers 3, 8, 21, 55, etc. to compute the scaling ratios, because the Fibonacci sequence is not a geometric sequence.

#### The exponential sequence

- Practical tool: use a geometric sequence of powers of the logarithmic constant  $e = 2.72$ , which determines the shape of animal horns, shells, etc.
- $e^2 = 7.39$ ,  $e^3 = 20.1$ ,  $e^4 = 54.6$ ,  $e^5 = 148$
- This geometric sequence is approximately equal to the universal scaling sequence, but differs in the larger terms

### **1.2. Universal Scaling.**

#### Constraints

- Constraints make design easier by narrowing down choices
- There are several constraints that guide design to adapt towards innate (biologically-

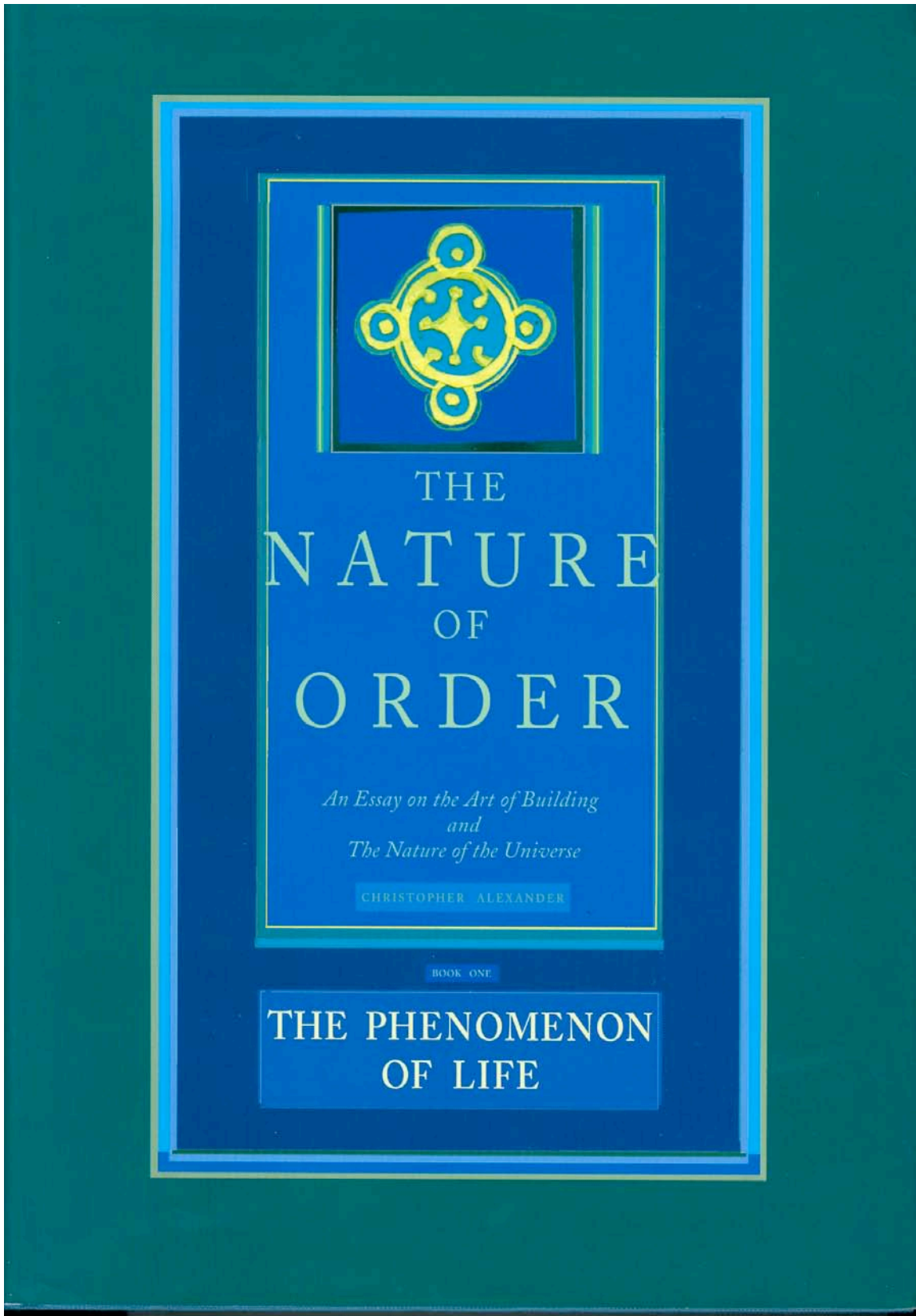
based) human sensibilities

- Universal scaling is a necessary but not sufficient condition for adaptive design

#### Universal scaling hierarchy

- Extends the old “rule of 3” used in the past, by giving all the other terms
- See “A Theory of Architecture”, Umbau-Verlag, Solingen, Germany, 2006: Chapters 2 & 3.
- Develops earlier results by Christopher Alexander in “The Nature of Order, Book 1”, Center for Environmental Structure, Berkeley, California, 2002.





*Christopher Alexander's "The Nature of Order, Book 1"*



With the new-found capacity of information handling systems, science is revealing truths about our world that were heretofore incalculable. From within this new body of knowledge we can better explain how the world around us works. In this book Dr. Salingaros answers a series of age-old questions about how we operate within the built environment, revealing the underlying structure of what is good architecture. His book gives insight and direction that can lead us to build a better place. For those among us, i.e. students, professors and practicing architects, who are seeking a more real manner in which to conceive of and construct architecture, I would recommend not one but two or even three thorough readings, without ideological prejudice, of:

**NIKOS A. SALINGAROS** A THEORY OF  
**ARCHITECTURE**

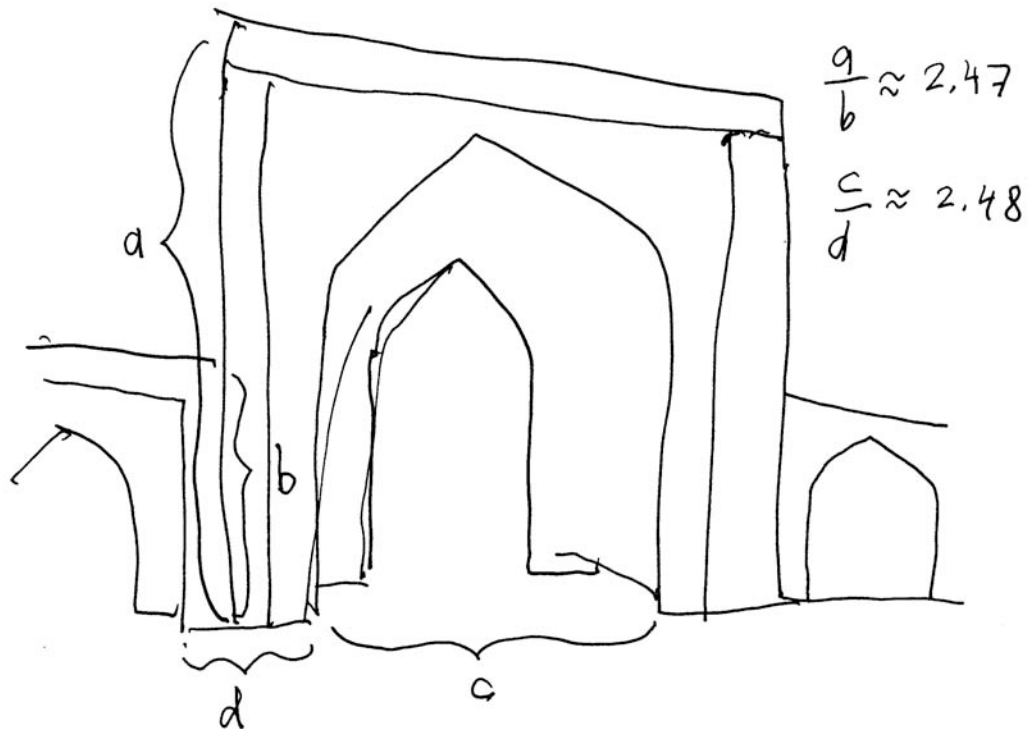
## *A Theory of Architecture*

### The Golden Mean

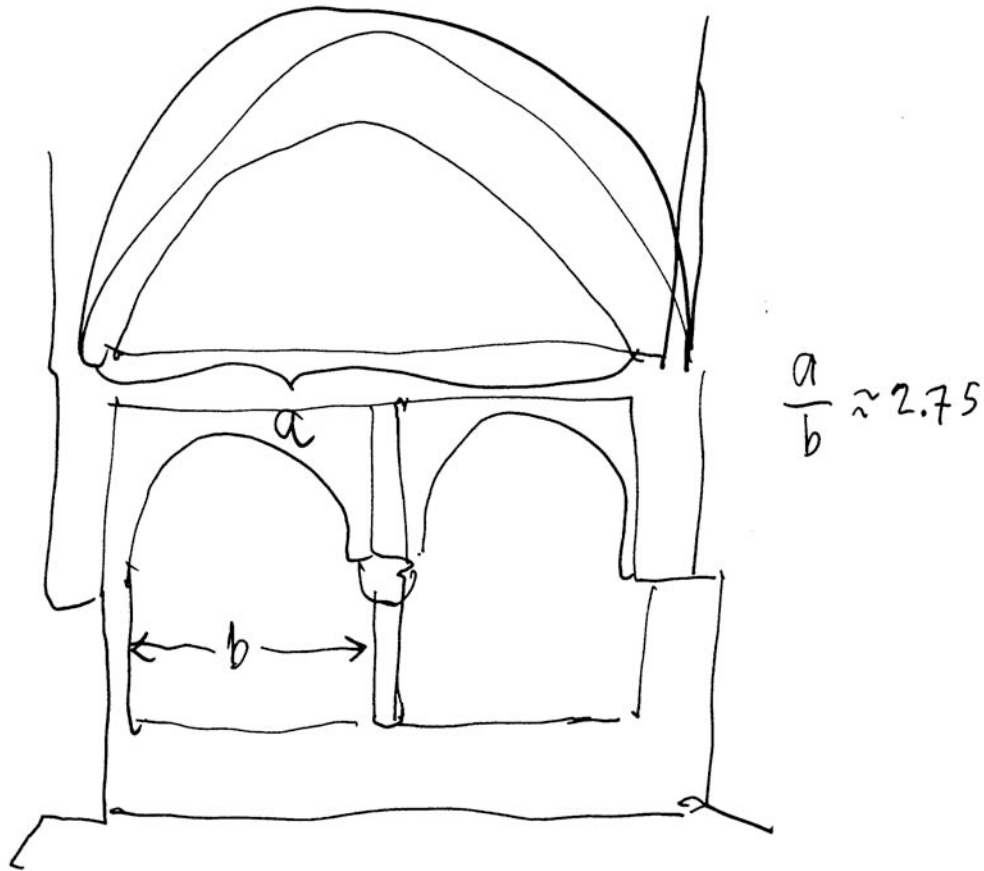
- It so happens that universal scaling is related to the square of the golden mean  $\Phi$   
 $\Phi^2 = \Phi + 1 = 2.618$
- This interesting coincidence has nothing to do with the proportions of rectangles, such as credit cards, the front elevation of the Parthenon, and other buildings!

### Architectures that obey universal scaling

- Gothic Architecture
- Classical Western Architecture
- Islamic Architecture
- Vernacular architectures the world over
- Traditional architectures from all cultures and all periods
- NOT international modernism



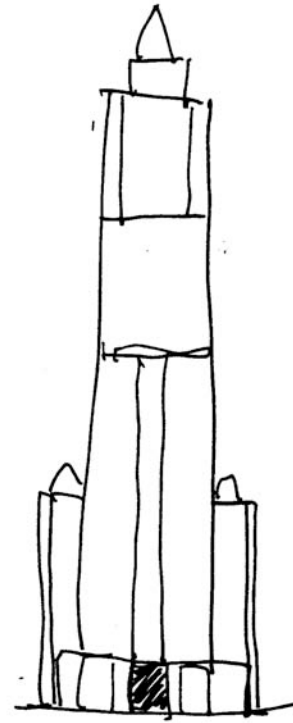
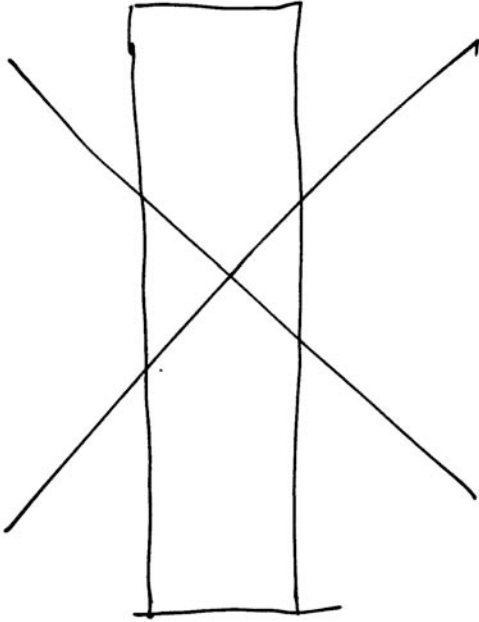
*Masjid-i-Shah, Isfahan*



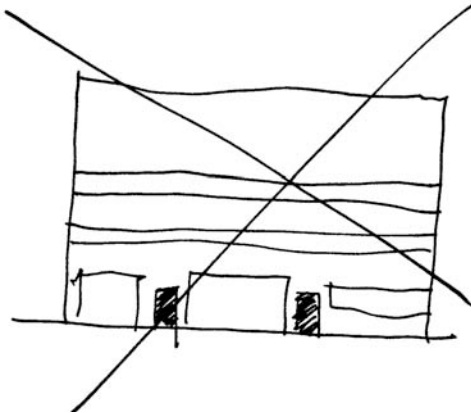
*Alhambra, Granada*

Validation from evolution

- All the cultures we know evolved universal scaling in their indigenous architectures, both vernacular and monumental
- Universal scaling is therefore innate
- The exceptions are military fortifications and the Pyramids, which had to appear unapproachable from the outside



*Application to skyscrapers*

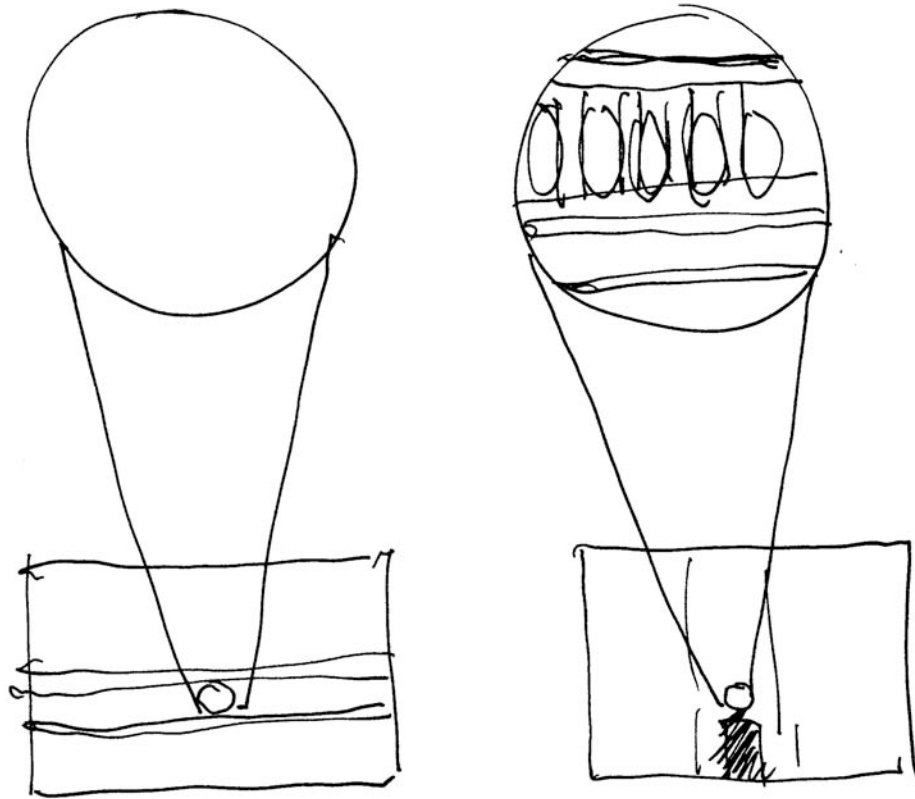


*Application to house façades*

The smaller scales

- The comparison we just did with two residences of roughly the same size and shape is seen on only the larger scales

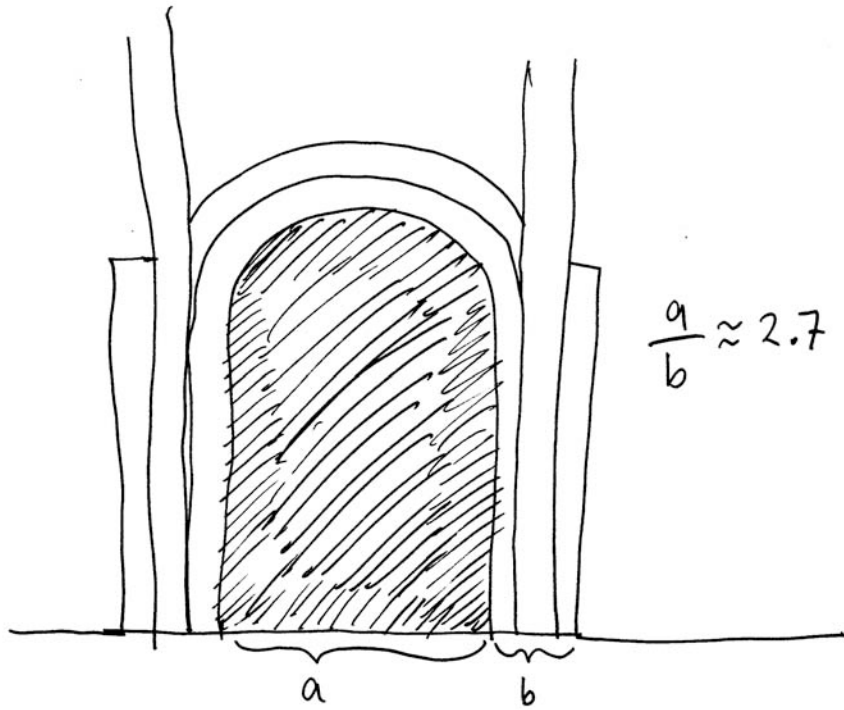
- But it is on the smaller scales that the difference is really dramatic
- In the modernist house, there are no smaller scales, thus no scaling hierarchy



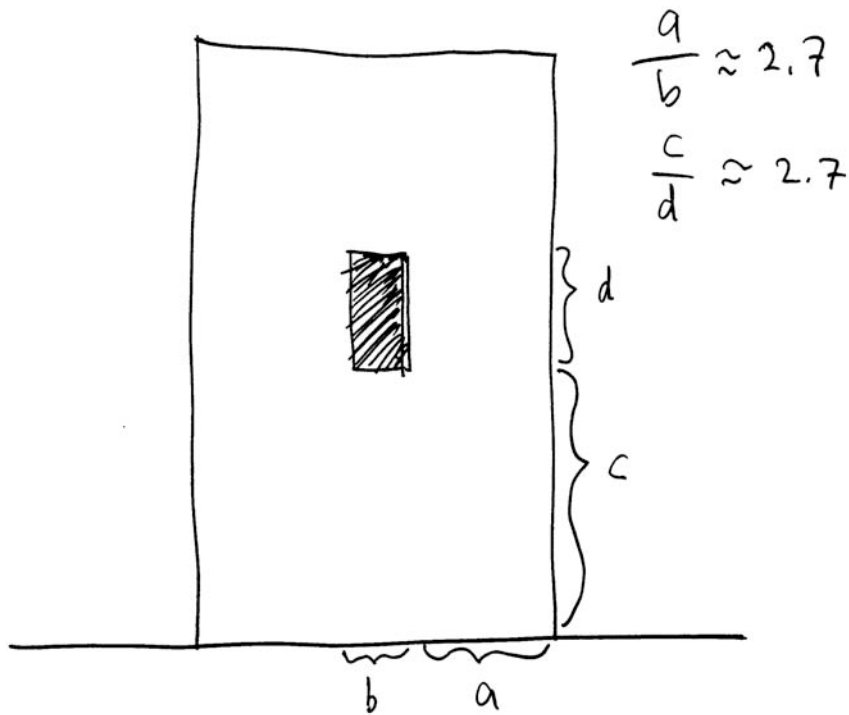
*Magnification*

Application: wide boundaries

- An articulation needs its edge defined
- Commensurate with universal scaling, edges or centers should have a lip
- This gives us wide door and window frames, baseboards, pilasters
- There is no longer a need to show off industrial materials without supports



*Wide door frame*



*Center follows scaling*

#### Summary

- Use ratios of lengths to aid design
- Change in thinking about “proportion”
- NOT the ratio of the sides of a rectangle, but compare instead dimensions of objects measured along the same direction
- Nothing magical or mystical about this

### **1.3. Biophilia.**

#### What is Biophilia?

- Edward O. Wilson used the term to describe an innate connection between all living beings
- More specifically, human beings have a biologically-founded link to other life-forms
- The connection is genetic — it resides in the common parts of our DNA

#### Human sensory systems

- Have evolved to respond to natural geometries of fractals, colors, scaling, symmetries
- Fine-tuned to perceive positive aspects (food, friends, mates) and threats
- Also fine-tuned to detect pathologies of our body, signaled by the departure from



natural geometries

### Biophilia and Health

- Human beings require contact with the geometry of biological structures
- Experiments in hospitals show much faster post-operative healing in rooms looking out at trees
- Social and mental health deteriorates in nature-less surroundings

### Healthy environments

- A healthy mind in a healthy body — which is situated in a healthy environment!
- Positive emotional response to the environment reduces stress and thus raises resistance to disease (external & internal)
- Emotional regeneration: the feelings inside a great Mosque, Cathedral, or Temple

### Universal scaling today

- Traditional architects use universal scaling intuitively, but very few people can get this kind of training today
- The memory of Classical architectural typologies is enough to guide the designer doing a traditional Classical building
- The problem is with design outside a traditional form language